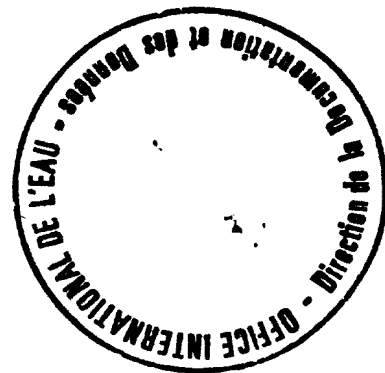


William A. Jury
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Transfer Functions and Solute Movement through Soil

Theory and Applications



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